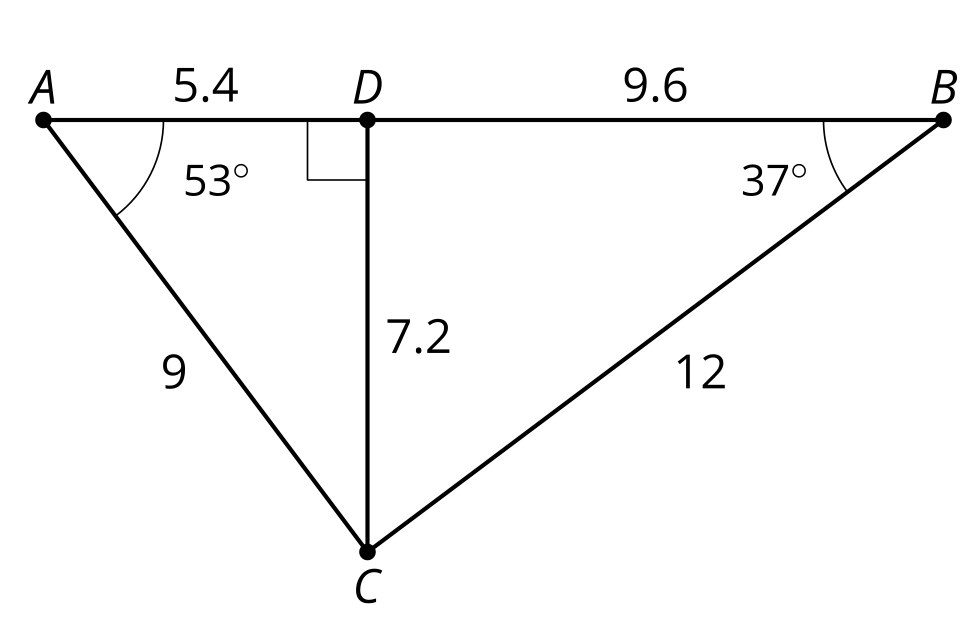
## Lesson 13: Using the Pythagorean Theorem and Similarity

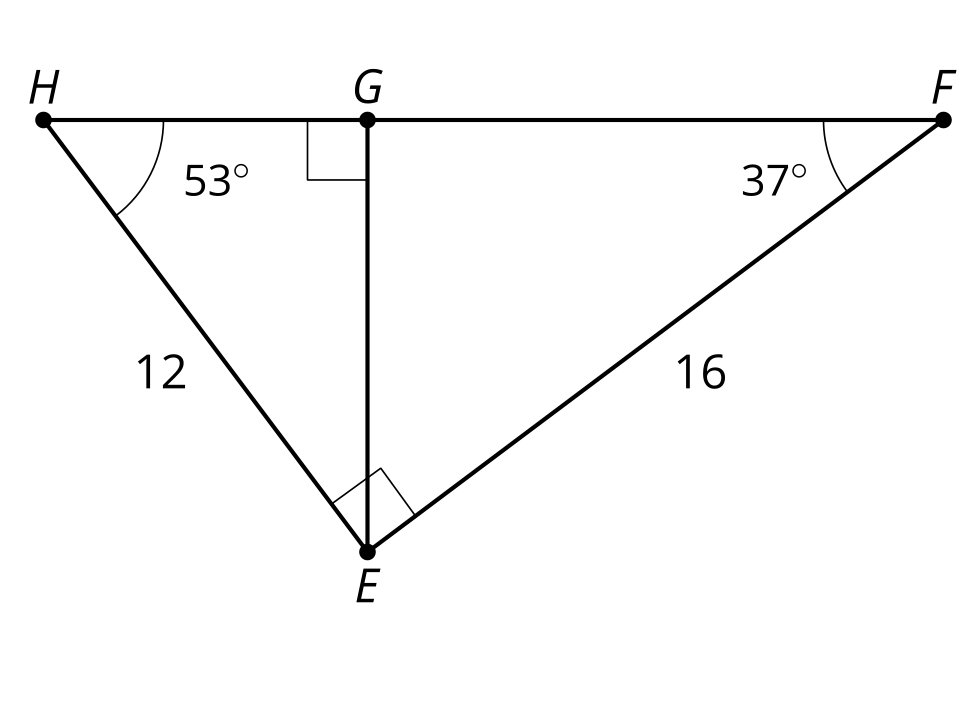
* Let’s explore right triangles with altitudes drawn to the hypotenuse.

### 13.1: Similar, Right?

Is triangle similar to triangle ? Explain or show your reasoning.



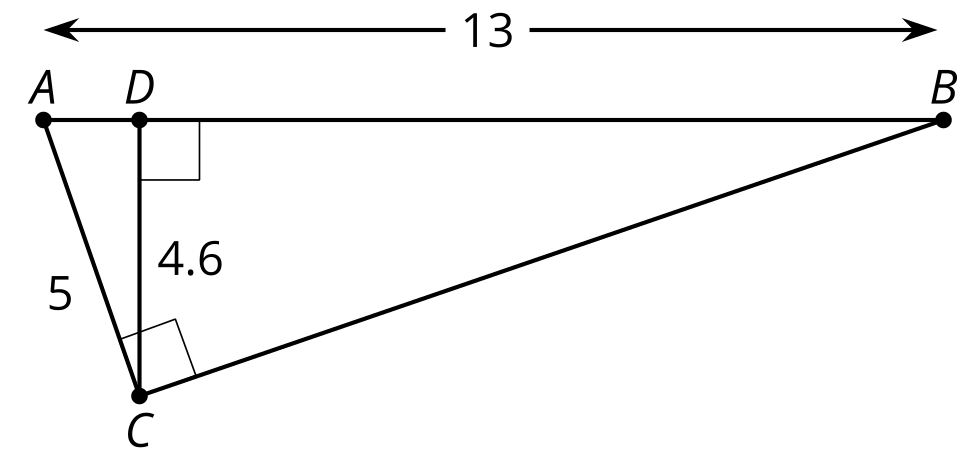
### 13.2: Tangled Triangles



Trace the 2 smaller triangles onto separate pieces of tracing paper.

1. Turn your tracing paper and convince yourself all 3 triangles are similar.
2. Write 3 similarity statements.
3. Determine the scale factor for each pair of triangles.
4. Determine the lengths of sides , , and .

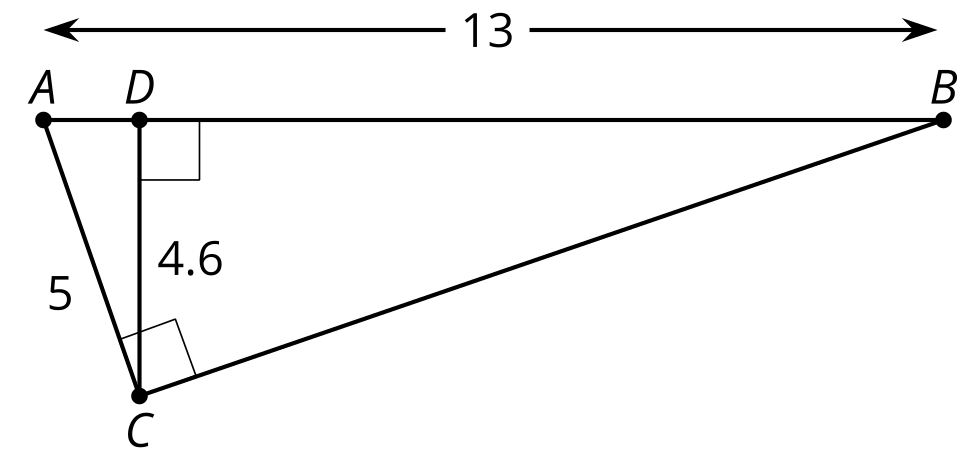
### 13.3: More Tangled Triangles



1. Convince yourself there are 3 similar triangles. Write a similarity statement for the 3 triangles.
2. Write as many equations about proportional side lengths as you can.
3. What do you notice about these equations?

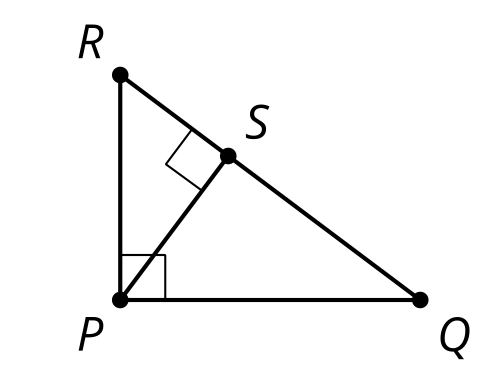
#### Are you ready for more?

Tyler says that since triangle is similar to triangle , the length of is 11.96. Noah says that since is a right triangle, we can use the Pythagorean Theorem. So the length of is 12 exactly. Do you agree with either of them? Explain or show your reasoning.

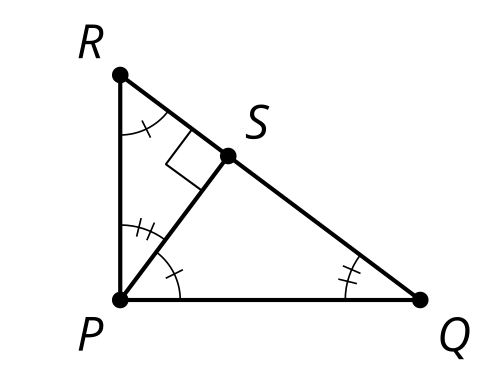


### Lesson 13 Summary

When we draw an **altitude** from the hypotenuse of a right triangle, we get lots of similar triangles that can be used to find missing lengths. An altitude is a segment from one vertex of the triangle to the line containing the opposite side that is perpendicular to the opposite side. For right triangle  we can draw the altitude **.**



Why are triangles , , and  all similar to each other?



Triangles and are similar by the Angle-Angle Triangle Similarity Theorem because angle is in both triangles, and both triangles are right triangles, so angles and are congruent. Triangles and are similar by the Angle-Angle Triangle Similarity Theorem because angle is in both triangles, and both triangles are right triangles, so angles and are congruent. Because triangles and are both similar to triangle , they are also similar to each other.

Since the triangles , , and are all similar, corresponding angles are congruent and pairs of corresponding sides are scaled copies of each other, by the same scale factor. We can use the proportionality of pairs of corresponding side lengths to find missing side lengths. For example, suppose we need to find and know and . Since triangle is similar to triangle , we know . So and . Or, suppose we need to find and know and . Since triangle is similar to triangle , we know . So and .



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