

Lesson 13: Expressions with Rational Numbers

Let's develop our signed number sense.

13.1: True or False: Rational Numbers

Decide if each statement is true or false. Be prepared to explain your reasoning.

1. $(-38.76)(-15.6)$ is negative

2. $10,000 - 99,999 < 0$

3. $\left(\frac{3}{4}\right)\left(-\frac{4}{3}\right) = 0$

4. $(30)(-80) - 50 = 50 - (30)(-80)$

13.2: Card Sort: The Same But Different

Your teacher will give you a set of cards. Group them into pairs of expressions that have the same value.

13.3: Near and Far From Zero

| a | b | $-a$ | $-4b$ | $-a + b$ | $a \div -b$ | a^2 | b^3 |
|----------------|----------------|------|-------|----------|-------------|-------|-------|
| $-\frac{1}{2}$ | 6 | | | | | | |
| $\frac{1}{2}$ | -6 | | | | | | |
| -6 | $-\frac{1}{2}$ | | | | | | |

1. For each set of values for a and b , evaluate the given expressions and record your answers in the table.

2. When $a = -\frac{1}{2}$ and $b = 6$, which expression:

has the largest value? has the smallest value? is the closest to zero?

3. When $a = \frac{1}{2}$ and $b = -6$, which expression:

has the largest value? has the smallest value? is the closest to zero?

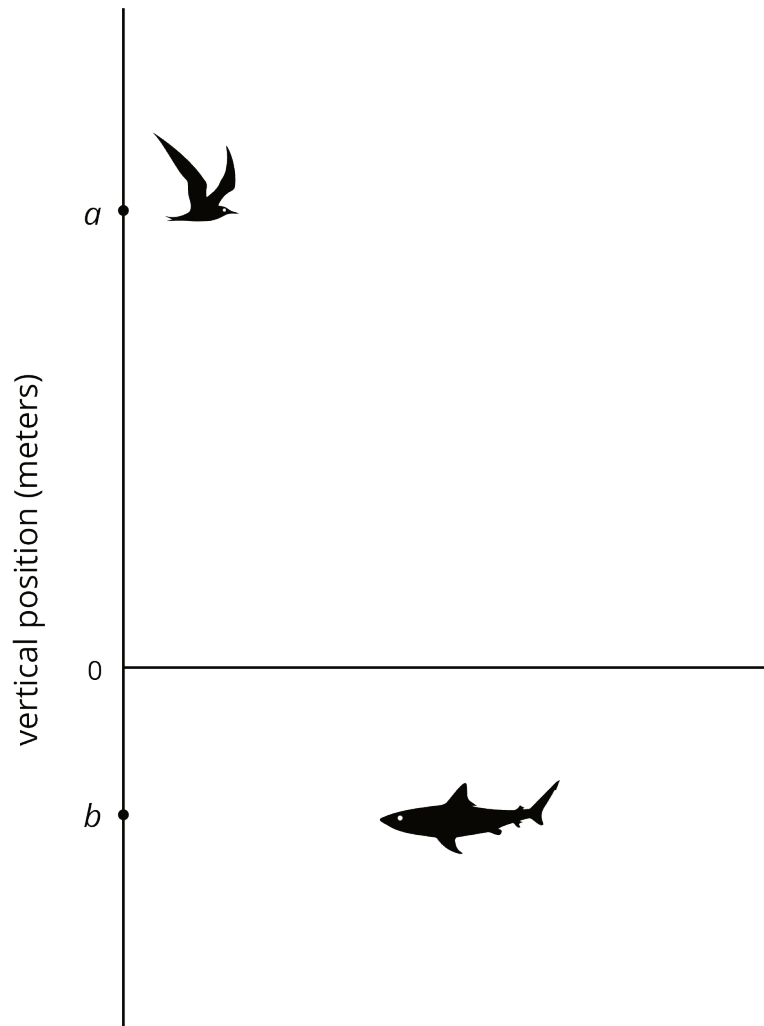
4. When $a = -6$ and $b = -\frac{1}{2}$, which expression:

has the largest value? has the smallest value? is the closest to zero?

Are you ready for more?

Are there any values could you use for a and b that would make all of these expressions have the same value? Explain your reasoning.

13.4: Seagulls and Sharks Again



A seagull has a vertical position a , and a shark has a vertical position b . Draw and label a point on the vertical axis to show the vertical position of each new animal.

1. A dragonfly at d , where $d = -b$
2. A jellyfish at j , where $j = 2b$
3. An eagle at e , where $e = \frac{1}{4}a$.
4. A clownfish at c , where $c = \frac{-a}{2}$
5. A vulture at v , where $v = a + b$
6. A goose at g , where $g = a - b$

Lesson 13 Summary

We can represent sums, differences, products, and quotients of **rational numbers**, and combinations of these, with numerical and algebraic expressions.

| Sums: | Differences: | Products: | Quotients: |
|--------------------|--------------------|---------------------|-----------------------|
| $\frac{1}{2} + -9$ | $\frac{1}{2} - -9$ | $(\frac{1}{2})(-9)$ | $\frac{1}{2} \div -9$ |
| $-8.5 + x$ | $-8.5 - x$ | $-8.5x$ | $\frac{-8.5}{x}$ |

We can write the product of two numbers in different ways.

- By putting a little dot between the factors, like this: $-8.5 \cdot x$.
- By putting the factors next to each other without any symbol between them at all, like this: $-8.5x$.

We can write the quotient of two numbers in different ways as well.

- By writing the division symbol between the numbers, like this: $-8.5 \div x$.
- By writing a fraction bar between the numbers like this: $\frac{-8.5}{x}$.

When we have an algebraic expression like $\frac{-8.5}{x}$ and are given a value for the variable, we can find the value of the expression. For example, if x is 2, then the value of the expression is -4.25 , because $-8.5 \div 2 = -4.25$.