

# Lesson 5: Efficiently Solving Inequalities

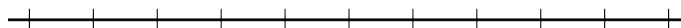
Let's solve more complicated inequalities.

## 5.1: Lots of Negatives

Here is an inequality:  $-x \geq -4$ .

1. Predict what you think the solutions on the number line will look like.
  
2. Select **all** the values that are solutions to  $-x \geq -4$ :
  - a. 3
  - b. -3
  - c. 4
  - d. -4
  - e. 4.001
  - f. -4.001

3. Graph the solutions to the inequality on the number line:

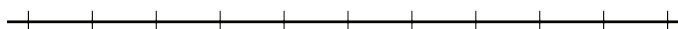


## 5.2: Inequalities with Tables

1. Let's investigate the inequality  $x - 3 > -2$ .

$x$	-4	-3	-2	-1	0	1	2	3	4
$x - 3$	-7		-5				-1		1

- a. Complete the table.
- b. For which values of  $x$  is it true that  $x - 3 = -2$ ?
- c. For which values of  $x$  is it true that  $x - 3 > -2$ ?
- d. Graph the solutions to  $x - 3 > -2$  on the number line:



2. Here is an inequality:  $2x < 6$ .

a. Predict which values of  $x$  will make the inequality  $2x < 6$  true.

b. Complete the table. Does it match your prediction?

$x$	-4	-3	-2	-1	0	1	2	3	4
$2x$									

c. Graph the solutions to  $2x < 6$  on the number line:



3. Here is an inequality:  $-2x < 6$ .

a. Predict which values of  $x$  will make the inequality  $-2x < 6$  true.

b. Complete the table. Does it match your prediction?

$x$	-4	-3	-2	-1	0	1	2	3	4
$-2x$									

c. Graph the solutions to  $-2x < 6$  on the number line:



d. How are the solutions to  $2x < 6$  different from the solutions to  $-2x < 6$ ?

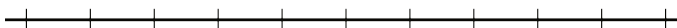
### 5.3: Which Side are the Solutions?

1. Let's investigate  $-4x + 5 \geq 25$ .

a. Solve  $-4x + 5 = 25$ .

b. Is  $-4x + 5 \geq 25$  true when  $x$  is 0? What about when  $x$  is 7? What about when  $x$  is -7?

c. Graph the solutions to  $-4x + 5 \geq 25$  on the number line.



2. Let's investigate  $\frac{4}{3}x + 3 < \frac{23}{3}$ .

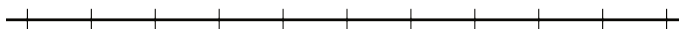
a. Solve  $\frac{4}{3}x + 3 = \frac{23}{3}$ .

b. Is  $\frac{4}{3}x + 3 < \frac{23}{3}$  true when  $x$  is 0?

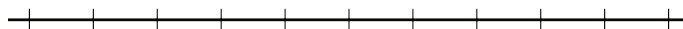
c. Graph the solutions to  $\frac{4}{3}x + 3 < \frac{23}{3}$  on the number line.



3. Solve the inequality  $3(x + 4) > 17.4$  and graph the solutions on the number line.



4. Solve the inequality  $-3\left(x - \frac{4}{3}\right) \leq 6$  and graph the solutions on the number line.



### Are you ready for more?

Write at least three different inequalities whose solution is  $x > -10$ . Find one with  $x$  on the left side that uses a  $<$ .

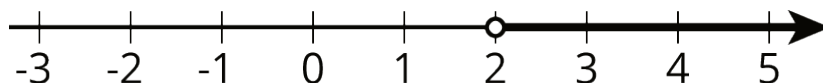
### Lesson 5 Summary

Here is an inequality:  $3(10 - 2x) < 18$ . The solution to this inequality is all the values you could use in place of  $x$  to make the inequality true.

In order to solve this, we can first solve the related equation  $3(10 - 2x) = 18$  to get the solution  $x = 2$ . That means 2 is the boundary between values of  $x$  that make the inequality true and values that make the inequality false.

To solve the inequality, we can check numbers greater than 2 and less than 2 and see which ones make the inequality true.

Let's check a number that is greater than 2:  $x = 5$ . Replacing  $x$  with 5 in the inequality, we get  $3(10 - 2 \cdot 5) < 18$  or just  $0 < 18$ . This is true, so  $x = 5$  is a solution. This means that all values greater than 2 make the inequality true. We can write the solutions as  $x > 2$  and also represent the solutions on a number line:



Notice that 2 itself is not a solution because it's the value of  $x$  that makes  $3(10 - 2x)$  equal to 18, and so it does not make  $3(10 - 2x) < 18$  true.

For confirmation that we found the correct solution, we can also test a value that is less than 2. If we test  $x = 0$ , we get  $3(10 - 2 \cdot 0) < 18$  or just  $30 < 18$ . This is false, so  $x = 0$  and all values of  $x$  that are less than 2 are not solutions.