Lesson 17: Quadratic Meanings

• Let's explore the meaning of quadratics.

17.1: Area Between Triangles



The area of the shaded region from the image can be represented by the expression $\frac{1}{2}(2+2a)(2+2a) - \frac{1}{2} \cdot 2^2$ which can be rearranged to $2a^2 + 4a$. To find the value of a when the shaded area is 30 square centimeters, Mai sets up the equation $2a^2 + 4a = 30$.

- 1. One solution to the equation is a = -5. Find another solution. Explain or show your reasoning.
- 2. What do the 2 solutions to the equation represent in this situation? Do the values make sense?

17.2: Getting the Ball Off the Roof

A ball is kicked off the roof of a building so that its height above the ground, given in feet, *t* seconds after it is kicked is represented by the equation $h(t) = -16t^2 + 33t + 37$.

1. At what height is the ball when it is kicked? Explain or show your reasoning.

2. At what height is the ball 2 seconds after it is kicked? Explain or show your reasoning.

- 3. What does it mean for the situation when h(t) = 8?
- 4. What does it mean for the situation when t = 1.3?
- 5. Graph the function.
 - a. Approximate the number of seconds after the ball is kicked when it will hit the ground. Explain how you know.
 - b. Approximate the number of seconds after the ball is kicked when it will reach its highest point. Explain how you know.
 - c. Approximate the number of seconds after the ball is kicked when it will reach its starting height again. Explain how you know.
- 6. Write an equation that represents the exact moment when the ball hits the ground.



17.3: Kicking the Field Goal

Andre kicks a football for a field goal. The height above ground, given in feet, *t* seconds after it is kicked, is represented by the equation $g(t) = -16t^2 + 56t + 0.5$.

1. At what height is the ball when it is kicked? Explain or show your reasoning.

2. At what height is the ball 2 seconds after it is kicked?

3. What does it mean for the situation when g(t) = 10?

- 4. What does it mean for the situation when t = 1.7?
- 5. Graph the function.
 - a. Approximate the number of seconds after the ball is kicked when it will hit the ground. Explain how you know.
 - b. Approximate the number of seconds after the ball is kicked when it will reach its highest point. Explain how you know.
 - c. Approximate the number of seconds after the ball is kicked when it will be 10 feet above the ground for the second time. Explain how you know.
- 6. Write an equation that would give the exact time when the ball is 10 feet above the ground.