# Unit 7 Lesson 21: Odd and Even Numbers

## 1 Math Talk: Evens and Odds (Warm up)

### Student Task Statement

Evaluate mentally.

64 + 88

65 + 89

14 · 5

14 • 4

### 2 Always Even, Never Odd

#### **Student Task Statement**

Here are some statements about the sums and products of numbers. For each statement:

- decide whether it is *always* true, true for *some* numbers but not others, or *never* true
- use examples to explain your reasoning
- 1. Sums:
  - a. The sum of 2 even numbers is even.
  - b. The sum of an even number and an odd number is odd.
  - c. The sum of 2 odd numbers is odd.
- 2. Products:
  - a. The product of 2 even numbers is even.
  - b. The product of an even number and an odd number is odd.
  - c. The product of 2 odd numbers is odd.

### 3 Even + Odd = Odd

#### **Student Task Statement**

How do we know that the sum of an even number and an odd number *must* be odd? Examine this proof and answer the questions throughout.

Let *a* represent an even number, *b* represent an odd number, and *s* represent the sum a + b.

1. What does it mean for a number to be even? Odd?

Assume that *s* is even, then we will look for a reason the original statement cannot be true. Since *a* and *s* are even, we can write them as 2 times an integer. Let a = 2k and s = 2m for some integers *k* and *m*.

2. Can this always be done? To convince yourself, write 4 different even numbers. What is the value for k for each of your numbers when you set them equal to 2k?

Then we know that a + b = s and 2k + b = 2m.

Divide both sides by 2 to get that  $k + \frac{b}{2} = m$ .

Rewrite the equation to get  $\frac{b}{2} = m - k$ .

Since *m* and *k* are integers, then  $\frac{b}{2}$  must be an integer as well.

- 3. Is the difference of 2 integers always an integer? Select 4 pairs of integers and subtract them to convince yourself that their difference is always an integer.
- 4. What does the equation  $\frac{b}{2} = m k$  tell us about  $\frac{b}{2}$ ? What does that mean about *b*?
- 5. Look back at the original description of *b*. What is wrong with what we have discovered?

The logic for everything in the proof works, so the only thing that could've gone wrong was our assumption that *s* is even. Therefore, *s* must be odd.