

Lesson 4: Solving for Unknown Angles

Let's figure out some missing angles.

4.1: True or False: Length Relationships

Here are some line segments.



Decide if each of these equations is true or false. Be prepared to explain your reasoning.

$$CD + BC = BD$$

$$AB + BD = CD + AD$$

$$AC - AB = AB$$

$$BD - CD = AC - AB$$



4.2: Info Gap: Angle Finding

Your teacher will give you either a *problem card* or a *data card*. Do not show or read your card to your partner.

If your teacher gives you the *problem card*:

- 1. Silently read your card and think about what information you need to be able to answer the question.
- 2. Ask your partner for the specific information that you need.
- 3. Explain how you are using the information to solve the problem.
 - Continue to ask questions until you have enough information to solve the problem.
- 4. Share the *problem card* and solve the problem independently.
- 5. Read the *data card* and discuss your reasoning.

If your teacher gives you the *data card*:

- 1. Silently read your card.
- 2. Ask your partner "What specific information do you need?" and wait for them to ask for information.
 - If your partner asks for information that is not on the card, do not do the calculations for them. Tell them you don't have that information.
- 3. Before sharing the information, ask "Why do you need that information?"

 Listen to your partner's reasoning and ask clarifying questions.
- 4. Read the *problem card* and solve the problem independently.
- 5. Share the *data card* and discuss your reasoning.

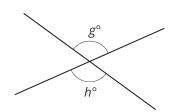
Pause here so your teacher can review your work. Ask your teacher for a new set of cards and repeat the activity, trading roles with your partner.



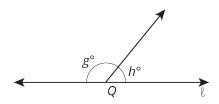
4.3: What's the Match?

Match each figure to an equation that represents what is seen in the figure. For each match, explain how you know they are a match.

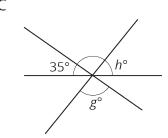
Α



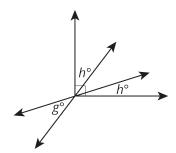
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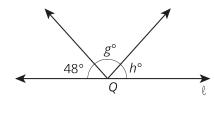
C



D



Ε



1.
$$g + h = 180$$

2.
$$g = h$$

$$3.2h + g = 90$$

$$4. g + h + 48 = 180$$

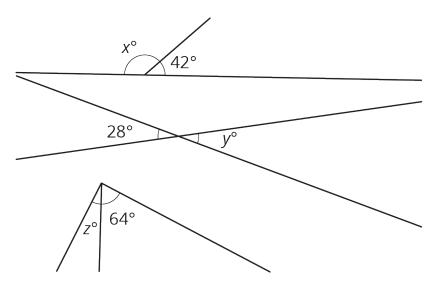
$$5. g + h + 35 = 180$$

Are you ready for more?

- 1. What is the angle between the hour and minute hands of a clock at 3:00?
- 2. You might think that the angle between the hour and minute hands at 2:20 is 60 degrees, but it is not! The hour hand has moved beyond the 2. Calculate the angle between the clock hands at 2:20.
- 3. Find a time where the hour and minute hand are 40 degrees apart. (Assume that the time has a whole number of minutes.) Is there just one answer?

Lesson 4 Summary

We can write equations that represent relationships between angles.



- The first pair of angles are supplementary, so x + 42 = 180.
- The second pair of angles are vertical angles, so y = 28.
- Assuming the third pair of angles form a right angle, they are complementary, so z + 64 = 90.